

Tutorial 3(TD3)

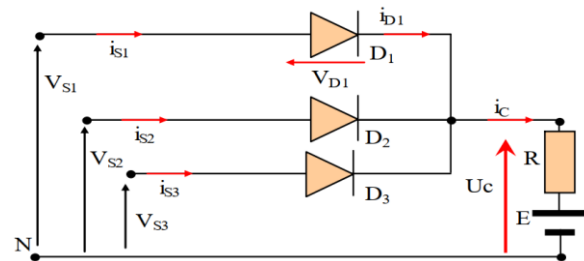
Example 1

The three-phase network 220/380, 50Hz is used to supply, through a single-phase rectifier, a load with an electromotive force (EMF) of $E=100V$ and a resistance of $R=50\Omega$.

$$v_1 = v_m \sin(\omega t),$$

$$v_2 = v_m \sin\left(\omega t - \frac{2\pi}{3}\right),$$

$$v_3 = v_m \sin\left(\omega t - \frac{4\pi}{3}\right)$$



Draw the curves U_c , V_{D2} , and i_c .

Calculate the average value of the rectified voltage and the average current in the load.

Provide the expression, calculate the average value, and plot the current $i_{s2}(t)$.

Calculate the power that the network must deliver.

Example 2

A DC motor operating at a constant torque is included in the circuit below

Represent the waveforms of u and u_k as functions of time.

Express the average value of u in terms of V and α .

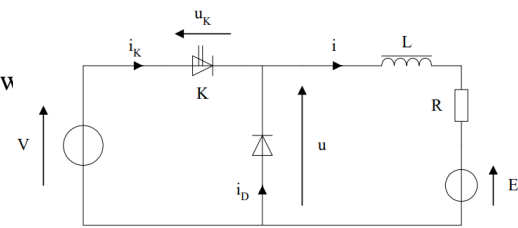
Illustrate the waveforms of i_k and i_D as functions of time.

Express the average values of currents i_k and i_D in terms of I and α .

Determine the current intensity I in the motor as a function of V , E , R , and ω .

Numerical application:

Calculate $\langle u \rangle$, I , and $\langle i_D \rangle$ for $V = 220 V$, $E = 145 V$, and $\alpha = 0.7$.



Example 3

We consider the parallel chopper circuit shown below, where T is the period, and α is the duty cycle.

1. $0 \leq t \leq \alpha T$: When the switch H is conducting. Write the differential equation governing the evolution of i . Assuming $i(0)=I_0$,

solve the equation to determine $i(t)$. Provide the expression for $I_1=i(\alpha T)$.

2. $\alpha T \leq t \leq T$: When the diode D is conducting. Keeping 0 as the time origin,

determine the expression for $i(t)$, particularly in terms of I_0

3. Assuming continuous current operation (i does not become zero over the interval $[\alpha T, T]$).

a) By stating that $i(T)=I_0$, derive the relationship between E , V , and α .

b) Sketch the shape of $i(t)$. Deduce its average value I_C in terms of I_0 and I_1 .

c) Let $\Delta i=I_1-I_0$. Express Δi in terms of E , L , α , and T .

d) Deduce from the two previous relations the expressions of I_0 and I_1 in terms of I_C and Δi .

e) Application: $E=200V$, $\alpha=0.25$, $L=5mH$, $I_C=10A$, $T=1ms$. Calculate I_0 , I_1 , and V , then plot the waveforms of i , i_H , i_D , and v_H .

